

## Matching a Wind Turbine with a Self-Excited Induction Generator

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**ABSTRACT:** This paper investigates an analytical approach for matching the characteristics of a fixed pitch angle wind turbine with that of a self-excited induction generator (SEIG). The generator feeds its stator electrical output power into an infinite bus-bar via a static power conditioner. The power conditioner used here consists of a diode bridge rectifier and an inverter bridge thyristor tied together through a d.c. link reactor of high inductance in the stator circuit. The analysis is carried out by representing the steady state performance of the self-excited induction generator mathematical model. The wind turbine's performance curve, power coefficient versus tip speed ratio,  $C_p(\lambda)$ , is represented by a polynomial function of both the generator speed and the wind speed. At any given generator speed the wind turbine output mechanical power is equated to the SEIG input mechanical power. From this mechanical power balance a non-linear equation for the wind speed is resulted. This equation is solved numerically using Newton-Raphson method. Knowing the wind speed the corresponding other performance characteristics can easily be obtained.

[Adel S. Nada and Saeed A. Al-Ghamdi. **Matching a Wind Turbine with a Self-Excited Induction Generator.** *J Am Sci* 2013;9(6):607-614]. (ISSN: 1545-1003). <http://www.jofamericanscience.org>. 77

**Key Words:** Wind turbine, Induction generator, Static power conditioner, Infinite bus-bar.

### 1. Introduction

The increasing energy demand throughout the world, the air pollution produced by fossil fuel as well as the limited reserves of this fuel and the growing doubt about the safety of nuclear power led to a growing demand for the wider use of renewable energy sources such as wind. Wind energy has the advantages that, it is clean and inexhaustible. Various schemes for generating electricity from wind have been proposed. One of these schemes is the SEIG connected to an infinite bus-bar using rectifier – dc link – inverter scheme in the stator circuit which is the subject of this paper. A three phase induction machine can be made to work as a self-excited induction generator (SEIG), when its rotor is driven at suitable speed and its stator terminals connected to a three phase capacitor bank to provide the necessary excitation. The induced e.m.f. and current in the stator windings will continue to rise until an equilibrium is attained due to the magnetic saturation in the machine.

The speed dependent stator voltage and frequency are interfaced with the network using a diode bridge rectifier and an inverter bridge thyristor tied together through a d.c. link reactor of high inductance. This energy conversion scheme has the following advantages:

*i-* It has no synchronizer and doesn't need pitch angle control. Hence, it is simple, easy to run, and cheap. Moreover, the absence of these devices reduces the weight of the turbine generator system which must be located on the top of the wind turbine tower.

*ii-* Because of the gust structure of the wind, and because of a cyclical variation in the turbine-blade loading caused by tower shadow and wind shear, severe mechanical and electrical stresses can be induced in the generator. Consequently, a rare or compliant damped coupling is usually interposed between the synchronous generator and the wind turbine. Johnson and Simth [1] suggested that, the use of an induction generator could be obviate the need for such coupling.

A capacitor self-excited induction generator (SEIG), has emerged as a suitable candidate of wind energy source because of its many advantages such as its small size and weight, robust construction, reduced unit and maintenance cost, brushless rotor construction, absence of a separate excitation source, and self-protection against severe over loads and short circuits [2]. It is widely known that an induction machine can self-excite when a suitable capacitance is connected across its stator terminals and the rotor is driven by a prime mover. Under such conditions, the terminal capacitance furnishes the lagging reactive power necessary for establishing the air gap flux. This phenomenon is termed the "capacitor self-excitation", which can be exploited to operate the induction machine as a generator. The induced voltages and currents would continue to rise, but for magnetic saturation in the machine which results in an equilibrium state being reached and the machine is often referred to a self-excited induction generator (SEIG) [3]. The steady state analysis and performance of the SEIG driven by regulated and unregulated turbines is discussed by Chan [4].

El-Sadek et al. [5] developed a control system for on-line simulation of wind turbine by separately excited d.c. motor and the SEIG performance with isolated load is derived. The wind electric energy conversion systems (WEECS) are classified based upon the type of turbine (fixed or variable pitch turbine) and the electric generator type. Constant speed is often obtained by using variable pitch turbines and the fixed turbines usually produce a variable speed [6]. An attempt has been made to present a simple model to control the output voltage and frequency in case of self-excited induction generator under varying wind speeds operation. [7]

Nasserredine [8] showed the advantages of using a Switched Reluctance Generator (SRG) for wind energy applications. The theoretical study of the self-excitation of a SRG and the determination of the variable parameters in a SRG design are discussed.

The power in the wind is proportional to the cube of the wind speed. The fractional power that can be extracted from the wind power by a wind turbine is usually given the symbol  $C_p$ . This symbol is called the performance or power coefficient of the turbine. The power coefficient depends on the wind speed, the rotational speed of the turbine, and turbine blade parameters such as pitch angle as well as the number of blades. In the system under study there is no need for pitch angle control [9]. The control is to be accomplished electrically by adjusting the inverter firing advance angle  $\beta$ . This paper presents an analytical approach for matching the steady state characteristics of a fixed pitch angle wind turbine with that of a SEIG connected to an infinite bus-bar. It is assumed here that, the machine is driven by wind energy and connected from its stator terminal to a unified network. The input mechanical power to the SEIG at any speed is computed using the equivalent circuit of the SEIG. Equating the mechanical power extracted from the wind with the input mechanical power to the SEIG results in a non-linear equation for the unknown wind speed. By solving this equation using Newton-Raphson method of iteration, we obtain the wind speed. Consequently the corresponding other performance quantities of the wind turbine such as power coefficient  $C_p$  and tip to wind speed ratio  $\lambda$  can easily be computed.

## 2. System Description

A simplified steady state analysis of a wind energy driven (SEIG) interfaced to an infinite bus bar using diode bridge - d.c. link reactor - inverter bridge scheme. Some simplifying assumptions are introduced to simplify the analysis. Concerning with the current converter, an ideally smooth current is assumed in the d.c. link. Moreover, the commutation is neglected in the inverter bridge.

Also, the self-excitation capacitor reduces the commutation in the rectifier bridge to such an extent, that it can be ignored with a very minor error. Concerning with the machine side only the fundamental current component is considered. The analysis is performed assuming the magnetizing reactance is constant at its maximum value.

Similar to the procedure described by Nada [9], the minimum value for the terminal capacitor needed for self-excitation is determined using the no load steady state equivalent circuit of SEIG, in terms of the maximum saturated magnetizing reactance and the other parameters together with a chosen suitable lowest speed. This obtained capacitance is used during loading conditions. Under load, the frequency of self-excitation at any given speed is computed assuming that, the input reactive power to the diode bridge is always zero, i.e., the generator operates always at unity power factor load. Newton-Raphson method is used for solving the nonlinear equation determining the frequency of self-excitation under load. A steady state mathematical model for the system under load conditions is derived. Different modes of operations are then investigated and the required control characteristic in each case is obtained. The speed dependent generated voltage is matched with that of the supply network by appropriate adjustment of the inverter firing advance angle  $\beta$ .

Figure 1 shows the single line diagram of the system under study with the different constituting parts. A diode bridge rectifier is preferably used to achieve an operation of the induction generator always at nearly unity power factor. The rectified direct current  $I_d$  is smoothed by a reactor of high inductance  $L_d$  acting as an intermediate circuit to decouple the machine and the a.c. supply network.

## 3. System Analysis

For an induction generator to be self-excited, the machine has to operate in the saturation region. Therefore, for a given speed and load, the terminal capacitor should have a value such that the magnetizing reactance always lies in the saturated region. Let  $X_m$  be the maximum saturated magnetizing reactance of the machine, which can be experimentally determined [2]. Even though the  $X_{ms}$  of the machine varies considerably with operating conditions (owing to saturation), the assumption of a single value  $X_m$  in the analysis is acceptable, because the minimum feasible capacitor value is inevitably associated with the lowest magnetizing KVAs and magnetizing current, which in turn corresponds to the maximum  $X_{ms}$  value. In practice, the maximum saturated magnetizing reactance value corresponds to an operating point very slightly above the linear part of the machine magnetization curve (where a stable operating point

is just feasible), and hence  $X_m$  will be very slightly less than the machine unsaturated magnetizing reactance [2,3].

In this paper, a suitable lowest speed is chosen. This speed should lie in the range above the generator cutoff speed. Hence, the steady state equivalent circuit of SEIG at no load is used to determine the corresponding minimum value of the terminal capacitance required for self-excitation in terms of the machine maximum saturated magnetizing reactance together with the other

parameters. This obtained capacitance is used during loading conditions. The frequency of self-excitation under load is computed on the basis of assuming that the input reactive power to the rectifier bridge is always zero. This assumption is justified by the use of a diode bridge rectifier. The rectified voltage behind the d.c. reactor is equated with that of the inverter bridge to get the necessary firing advance angle  $\beta$  of the inverter according to the machine speed.

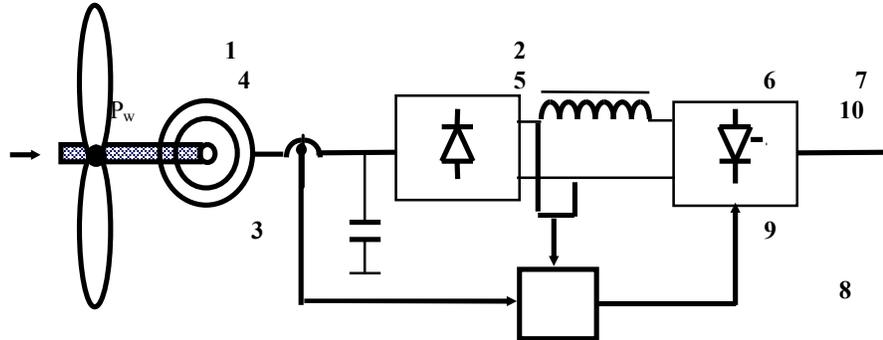


Fig. 1: Single line diagram of a wind energy driven SEIG connected to an infinite bus bar using a static power conditioner.

- |   |                             |    |                               |
|---|-----------------------------|----|-------------------------------|
| 1 | wind turbine                | 6  | inverter bridge               |
| 2 | 3-phase induction generator | 7  | supply network                |
| 3 | 3-phase capacitor bank      | 8  | control device                |
| 4 | rectifier bridge            | 9  | d.c. link voltage measurement |
| 5 | d.c. smoothing reactor      | 10 | stator current measurement    |

### 3.1 Determination of Self-Excitation Capacitor

The per phase steady state equivalent circuit of a self-excited induction generator under no load at rated frequency  $f_n$  is shown in Fig. 2 [10,11]. Here the machine core losses and saturation effect has been ignored. As there is no externally applied voltage, the mesh equations for the stator current  $I_s$  and referred rotor current  $I_r'$  are:

$$-\left[\frac{R_s}{F} + j(X_{\infty} - X_c / F^2)\right]I_s + jX_m(I_r' - I_s) = 0 \quad (1)$$

$$-[R_r' / (F - v) + jX_{\sigma r}']I_r' - jX_m(I_r' - I_s) = 0 \quad (2)$$

Where  $F = f/f_n$  is the per unit self-excitation frequency and  $v = n/n_s$  is the per unit speed. Eliminating  $I_s$  and  $I_r'$  from Eqs. (1) and (2) we find that:

$$[R_r' / (F - v) + jX_{\sigma r}']\left[\frac{R_s}{F} + (X_s - X_c / F^2)\right] + X_m^2 = 0 \quad (3)$$

Where the self-reactance of the stator  $X_s$  and the referred self-reactance of the rotor  $X_r'$  are:

$$X_s = X_{\infty} + X_m \quad (4a)$$

$$X_r' = X_{\sigma r}' + X_m \quad (4b)$$

Equating the real and imaginary parts to zero separately, yields:

$$\frac{R_s}{F} \cdot \frac{R_r'}{(F - v)} - X_r'(X_s - X_c / F^2) + X_m^2 = 0 \quad (5a)$$

$$\text{and: } \frac{R_s}{F} X_r' + \frac{R_r'}{(F - v)} (X_s - X_c / F^2) = 0 \quad (5b)$$

By solving Eqs. (5a) and (5b) for the per unit self-excitation frequency and the capacitive reactance  $X_c$  we obtain:

$$K_1 F^2 + K_2 F + K_3 = 0 \quad (6a)$$

and:

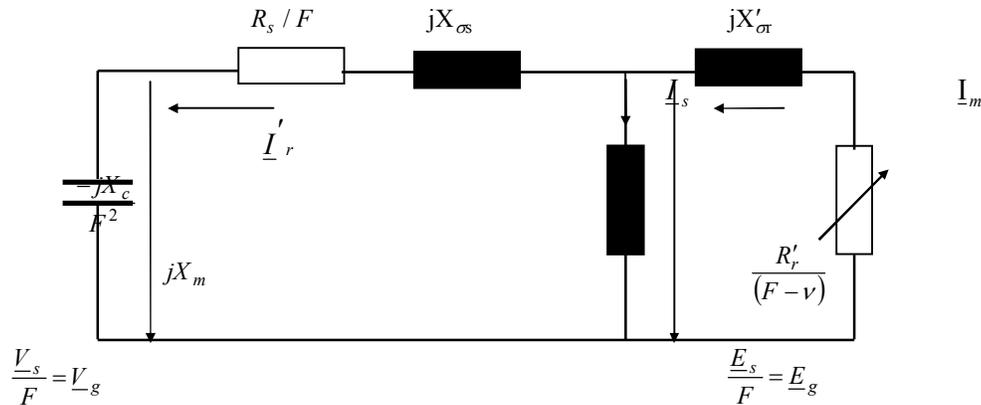


Fig. 2: Per phase steady state equivalent circuit of SEIG at no load.

$$X_c = K_4 F^2 + K_5 F \tag{6b}$$

Where the constants  $K_1 - K_5$  are dependent on the equivalent circuit parameters and the speed of the generator. These constants are:

$$\begin{aligned} K_1 &= X_m^2 + X_r'^2 R_s / R_r' \\ K_2 &= -v \cdot (X_m^2 + 2X_r'^2 R_s / R_r') \\ K_3 &= v^2 \cdot (X_r'^2 R_s / R_r') + R_s R_r' \\ K_4 &= X_s + X_r' R_s / R_r' \\ K_5 &= -v X_r' R_s / R_r' \end{aligned} \tag{7}$$

Solving the second order Eq. (6a) we obtain the maximum per unit self-excitation frequency as:

$$F_{max} = 0.5 \left[ -\frac{K_2}{K_1} + \sqrt{\left(\frac{K_2}{K_1}\right)^2 - 4 \frac{K_3}{K_1}} \right] \tag{8}$$

Introducing Eq. (8) into Eq. (6b), the corresponding minimum self-excitation capacitance can be found as:

$$C_{min} = \frac{1}{\omega_n \cdot [K_4 F_{max}^2 + K_5 F_{max}]} \tag{9}$$

with the generator rated angular frequency being:

$$\omega_n = 2\pi f_n \tag{10}$$

The generator cutoff speed  $V_{cutoff}$  below which there is no generation is attained when the quantity under the square root in Eq. (8) becomes zero. A speed below this value results in a complex root for the maximum per unit self-excitation frequency. Accordingly, we can write:

$$\left(\frac{K_2}{K_1}\right)^2 = 4 \frac{K_3}{K_1} \tag{11}$$

Introducing Eqs. (7) into the above equation yields:

$$v_{cutoff} = \frac{2}{X_m^2} \sqrt{R_s R_r' X_m^2 + R_s^2 X_r'^2} \tag{12}$$

Thus, choosing a suitable lowest value for the per unit speed  $v$  greater than or equal  $V_{cutoff}$ , the corresponding  $F_{max}$  can be computed using Eq. (8). Once  $F_{max}$  is obtained, the corresponding

minimum self-excitation capacitor  $C_{min}$  is determined from Eq. (9).

### 3.2 Determination of Self-Excitation Frequency Under Load

As stated before, the obtained  $C_{min}$  needed for self-excitation under no load, corresponding to the chosen lowest speed will be used under loading conditions. The per unit frequency  $F$  for self-excitation under load is determined by applying the assumption of unity power factor operation for the generator [3]. Combining this assumption together with the equivalent circuit of SEIG under load of Fig. 3 yields:

$$Q = \text{Imag.} \left\{ \underline{V}_g \cdot \underline{I}_L^* \right\} = 0 \tag{13}$$

where  $Q$  is the input reactive power to the rectifier bridge. Referring to the equivalent circuit of Fig. 3, the relation between the load current  $\underline{I}_L$ , the capacitor current  $\underline{I}_c$  and the stator current  $\underline{I}_s$ , is obtained as:

$$\begin{aligned} \underline{I}_L = -\underline{I}_c + \underline{I}_s = & \frac{-\underline{V}_g}{-jX_c} \\ & + \frac{-\underline{V}_g}{\frac{R_s}{F} + jX_{om} + \frac{jX_m [R_r' / (F-v) + jX_{or}']}{R_r' / (F-v) + jX_r'}} \end{aligned} \tag{14}$$

Where  $\underline{V}_g$  is the terminal generator voltage.

Introducing Eq. (14) into Eq.(13) we obtain the following relation for the per unit self-excitation frequency  $F$ :

$$C_1 F^4 + C_2 F^3 + C_3 F^2 + C_4 F + C_5 = 0 \tag{15}$$

The coefficients  $C_1$  through  $C_5$  are functions of the equivalent circuit parameters, the minimum self-excitation capacitor  $C_{min}$  and the generator speed. Equation (15) is solved numerically to obtain the per unit frequency  $F$  for self-excitation.

### 3.3 Performance Equations

As the per unit self-excitation frequency  $F$  is obtained, the complete behavior of the system under loading conditions can be determined as follows:

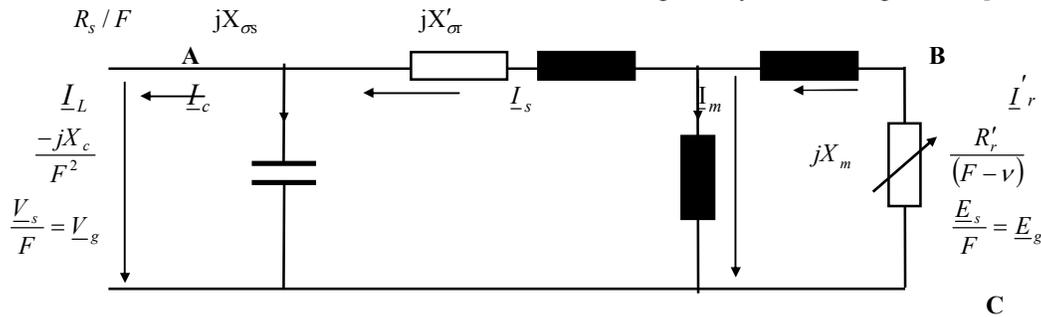


Fig. 3: Per phase steady state equivalent circuit of SEIG at load.

$$I_d = \frac{\pi}{\sqrt{6}} I_L \quad (16)$$

The matching relation between the generated machine voltage and the supply network a.c. voltage, considering the valves as ideal switches, is given by:

$$\frac{3\sqrt{6}}{\pi} V_g - R_{dc} I_d = \frac{3\sqrt{6}}{\pi} V_n \cos(\beta) \quad (17)$$

Where  $R_{dc}$  is the resistance of smoothing inductor and  $\beta$  is the inverter firing advance angle.

The power transferred to the supply network is given by:

$$P_g = \left[ \frac{3\sqrt{6}}{\pi} V_g - R_{dc} I_d \right] \cdot I_d = \frac{3\sqrt{6}}{\pi} V_n \cos(\beta) \cdot I_d \quad (18)$$

The total copper losses are computed from:

$$P_{cu} = P_{cs} + P_{cr} = 3(R_s I_s^2 + R'_r I_r'^2) \quad (19)$$

Adding Eqs. (18) and (19) yields the input internal mechanical power; thus:

$$P_{mg} = P_g + P_{cu} \quad (20)$$

Equations (14), and (16) to (20) represent the steady state performance equations describing the complete behavior of the system under different loading conditions.

### 3.4 Wind Turbine

The power available in wind is proportional to the cube of the wind speed. The fraction of the wind power that can be extracted by a wind turbine  $P_{mt}$  is proportional to the air density  $\rho$ , the area swept by the turbine  $A$ , the turbine performance coefficient  $C_p$ , and the cube of the wind speed  $V_w$ , we obtain [6,9]:

$$P_w = \frac{1}{2} \rho A V_w^3 \quad (21)$$

with  $\rho$  is the air density and  $A$  is the area swept by the turbine blade.

The mechanical power that can be extracted from the wind and which is available at the wind-

The load, the capacitor and the stator currents can be obtained from Eq. (14). The d.c. current  $I_d$  and the fundamental r.m.s. load current  $I_L$  are related together by the following relation [12-14]:

turbine shaft for driving the induction generator is given by:

$$P_{mw} = C_p \cdot P_w = C_p \cdot \frac{1}{2} \rho A V_w^3 \quad (22)$$

The wind turbine performance coefficient depends on the blades number and its pitch angle. For a certain number of blades with a certain pitch angle, the turbine performance coefficient varies with the blade tip speed  $V_T$  to the wind speed ratio  $\lambda$ . On the other hand the tip speed  $V_T$  is proportional to the rotor speed  $n$ , and the radius of the turbine blades  $R$ . Accordingly we can write:

$$\lambda = \frac{V_T}{V_w} = \frac{2\pi R n}{V_w} = \frac{1-S}{v_w} \quad (23)$$

Where the per unit wind speed  $v_w$  is given by:

$$v_w = \frac{V_w}{2\pi R n_s} \quad (24)$$

Figure 1 shows a typical  $C_p(\lambda)$  curve for a two blades wind turbine having a fixed pitch angle of  $1^\circ$  which is used for analysis in this paper [6]. Using curve fitting method the curve  $C_p(\lambda)$  shown in this figure could be approximated by a second order polynomial of the form [9]:

$$C_p = -0.007 \lambda^2 + 0.135 \lambda - 0.218 \quad (25)$$

The above approximation is shown dotted on the same Figure 4. Introducing Eq. (23) into (25) yields the power coefficient as:

$$C_p = -0.218 + 0.135 \left( \frac{1-S}{v_w} \right) - 0.007 \left( \frac{1-S}{v_w} \right)^2 \quad (26)$$

Grouping Eqs. (22) to (26) the turbine output mechanical power can be expressed as:

$$P_{mw} = K \cdot v_w^3 \cdot C_p = K \cdot C_p \left( \frac{1-S}{\lambda} \right)^3 \quad (27)$$

$$= K \left[ -0.218 v_w^3 + 0.135 (1-S) v_w^2 - 0.007 (1-S)^2 v_w \right]$$

with constant:

$$K = \frac{1}{2} \rho A (2\pi R n_s)^3 \quad (28)$$

The constant  $K$  can be computed by considering that the turbine is designed to achieve optimum value of  $C_{pmax}$  at rated wind speed  $v_{wn}$  corresponding to generator rated speed  $b_n$ . At this speed the generator input mechanical power is its rated value  $P_{mgn}$ . This power is calculated by solving the mathematical model of the electrical system at  $b_n$ . From Fig. 4, we have:

$$C_{pmax} = 0.43 \text{ at } \lambda_n = 9.35 \quad (29a)$$

By substituting  $P_{mw} = P_{mgn}$ ,  $C_p = C_{pmax}$ ,  $S = S_n$  and  $\lambda = \lambda_n$  into Eq. (27), the following relation for  $K$  is attained:

$$K = \frac{P_{mgn}}{C_{pmax}} \left( \frac{\lambda_n}{1-S_n} \right)^3 \quad (29b)$$

Finally, the turbine mechanical output power assumes the form:

$$P_{mw} = \frac{P_{mgn}}{C_{po}} \left( \frac{\lambda_o}{1-S_n} \right) \begin{bmatrix} -0.218 v_w^3 + 0.135(1-S)v_w^2 \\ -0.007(1-S)^2 v_w \end{bmatrix} \quad (30)$$

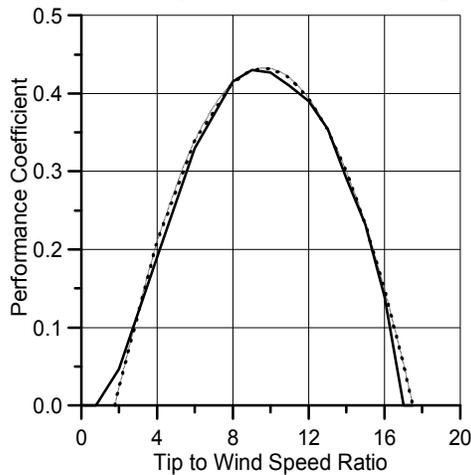


Fig. 4: Wind turbine performance curve, - - - - curve fitting approximation.

#### 4. Algorithm of Matching

At any given generator speed the generator input mechanical power  $P_{mg}$  is computed by solving the electrical system mathematical model during the speed range within which the given speed lies. At the same speed the determined generator input mechanical power  $P_{mg}$  is balanced by the turbine output mechanical power  $P_{mw}$  as in the equations (20) and (30).

Equation (30) represents a unified mathematical model for the wind turbine and the electrical system when they are connected together. It is solved using Newton-Raphson method of iteration for the unknown wind speed. Having obtained  $v_w$ , the corresponding required performance parameters  $\lambda$  and  $C_p$  of the turbine are determined using Eqs. (23) and (24).

#### 5. Predicted Steady State Characteristics

The following computed results are obtained from a 3-phase, 4-pole, 50-Hz, Y-connected, slip-ring induction machine. The machine has the following equivalent circuit parameters:

$$R_s = 2.22 \Omega, R'_r = 3.1 \Omega, X_{os} = X'_{or} = 5 \Omega, \text{ and } X_m = 74 \Omega.$$

The stator to rotor transformation ratio is 2.2

and the base values are:

$$\text{Base current, } I_b = 4.5 \text{ A, base voltage, } V_b = V_n = 220 \text{ V, and base power } P_b = 2970 \text{ W.}$$

#### 5.1 Terminal Capacitor Requirement

Using Eq. (9), the minimum self-excitation capacitance for different speeds can be obtained. As shown in figure 5, It is evident that the self-excitation capacitor sharply reduces as the speed rises. This means that a wider speed operating range is attained by using a higher capacitance value.

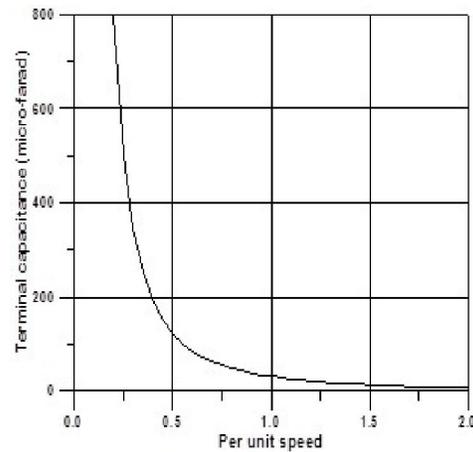


Fig. 5: Terminal capacitance versus per unit speed.

In the following results, the chosen lowest per unit speed  $v_{min} = 0.5$ , then the corresponding calculated minimum capacitance at no load  $C_{min} = 122.77 \mu\text{F}$ .

#### 5.2 Wind Turbine Requirements

The generator is driven by a wind turbine with a fixed pitch angle. Assuming the lowest per unit generator speed  $v_{min} = 0.5$  (according to the value of self-excitation capacitor used), the system is switched on to the power system. As the wind speed rises, the generator speed rises and its stator current should consequently increase. However, the inverter firing advance angle  $\beta$  is controlled according to the generator speed in such a way to keep the generated voltage constant at a certain maximum value (smaller than its rated value) until the stator current reaches its rated value. After this value of wind speed, the stator current is kept constant and equal to its rated value in order to prevent overloading the machine. The stator current is kept constant until the cut-off wind speed  $v_{wo}$  is reached. The generator

speed corresponding to  $v_{wo}$  is assumed here to be equal to twice its synchronous speed.

The obtained results are plotted in Figures 6 through 10. It is obvious that, there are two operating ranges:

i- The range from the cut-in wind speed  $v_{wi}$  to the rated wind speed  $v_{wn}$ :

Figure 6 shows the per unit self-excitation frequency as well as the per unit generator speed versus the per unit wind speed characteristics. The self-excitation frequency increases as the wind speed rises due to increasing the generator speed. During this range the tip to wind speed ratio  $\lambda$  should reduce from its largest value down to its optimum value  $\lambda_o$ . However, the performance coefficient  $C_p$  should rise from minimum value until its maximum value  $C_{po}$  as shown in Fig. 7. This means that the wind turbine should operate on right hand side of its characteristic as shown in Fig. 8 from the intersection point of  $C_p(\lambda)$  with the  $\lambda$  axis upwards to the point  $(\lambda_o, C_{po})$ . The generator input mechanical power (output mechanical power from the wind) and the generator electrical output power increase as the wind speed rises in this range as shown in Fig. 9. In this range, to maintain constant generated voltage the inverter firing advance angle  $\beta$  increases very slightly as shown in Fig. 10.

ii- The range from the rated wind speed to the cut-out wind speed  $v_{wo}$ :

During this range, the inverter firing advance angle  $\beta$  is increased to keep the stator current constant at its rated value. as shown in Fig. 10. This results in decreasing the mechanical input power as well as the output electrical power with the wind speed due to decreasing in stator voltage as shown in Fig. 9. Both the power coefficient and the tip to wind speed ratio decrease from the point  $(\lambda_o, C_{po})$  downwards on the left half of the curve  $C_p(\lambda)$  until the cut-out wind speed is reached.

**6. Conclusion**

An analytical approach for matching the characteristics of a wind turbine with that of a SEIG has been presented. The analysis is carried out by representing the steady state performance of the self-excited induction generator mathematical model. The wind turbine's performance curve, power coefficient versus tip speed ratio,  $C_p(\lambda)$ , is represented by a polynomial function of both the generator speed and the wind speed. At any given generator speed the wind turbine output mechanical power is equated to the SEIG input mechanical power. A unified model for the electrical system and the turbine is estimated from the mechanical power balance. This model is solved numerically using Newton-Raphson method to obtain the turbine

operating conditions under the specified SEIG control strategy.

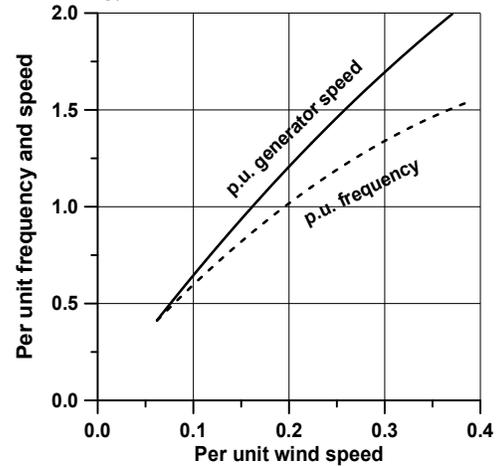


Fig. 6: Generator speed and frequency versus wind speed.

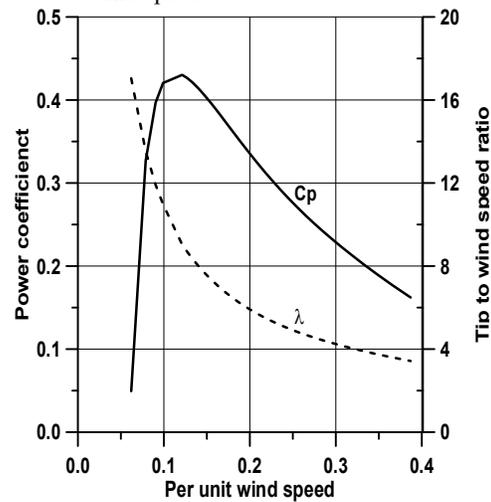


Fig. 7: Power coefficient and tip to wind speed ratio versus wind speed

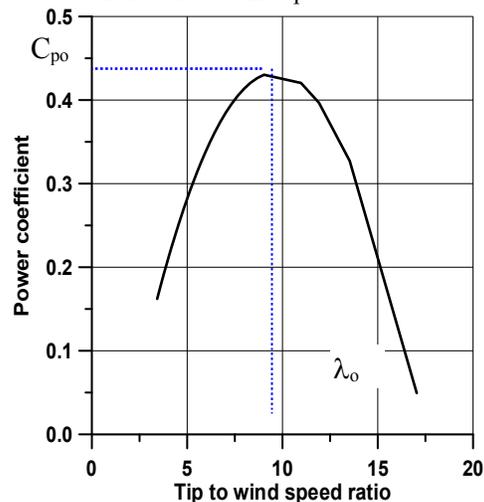


Fig. 8: Turbine operating range.

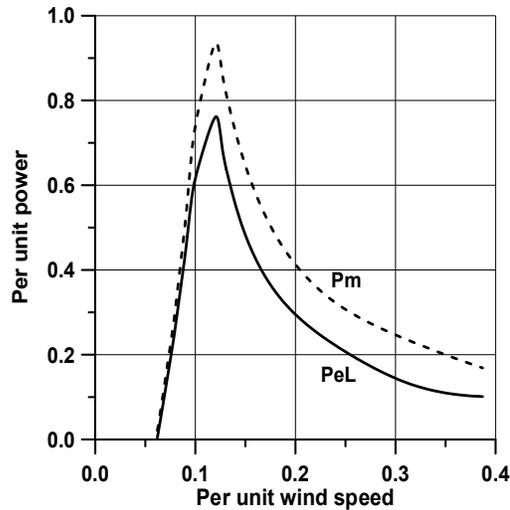
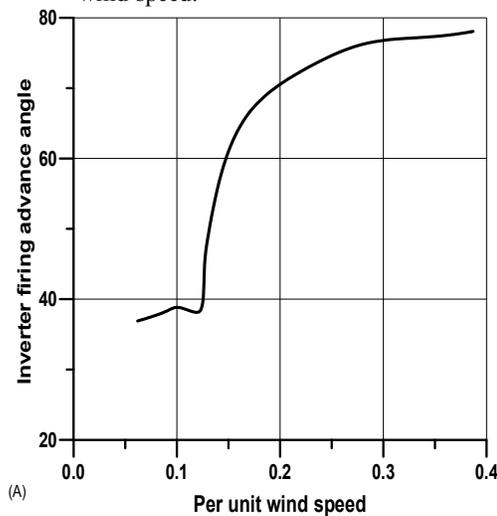


Fig. 9: Electrical and mechanical power versus wind speed.



(A)

Fig. 10: Inverter firing advance angle versus wind speed

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#### References

- Johnson, C.C. and Smith, R. T. :Dynamic of wind generators on electric utility networks, IEEE trans., Vol. AES-12, No. 4, July 1976, pp. 483-493.
- Al Jabri, A.K. and Alolah, A.I. : "Capacitance Requirement for Isolated Self Excited Induction Generator", IEE Proc. Vol. 137, Pt. B, No. 3, 1990, pp. 154-159.
- Chan, T.F.: "Steady State Analysis of Self Excited Induction Generators", IEEE Trans. on Energy Conversion, Vol. 9, No. 2, 1994, pp. 288-296.
- Chan, T.F. : "Self Excited Induction Generators Driven by Regulated and Unregulated Turbines", IEEE Trans. on Energy Conversion, Vol. 11, No. 2, June 1996, pp. 338-343.
- El-Sadek, M.Z., Saady, G. and Abdel-Mohsen, T.: "On-Line Simulation of Wind Turbine by Separately Excited DC Motor Driving Self Excited Induction Generator", Sixth Middle-East Systems Conference (MEPCON' 98), Mansoura, Egypt, 1998, pp. 105-109.
- Salameh, Z.M., and Kazda. : "A design Method for Matching the Characteristics of a Double Output Induction Generator (DOIG) with the Performance Characteristics of Wind Turbines", Proc. of the Midwest Power Conference, Nov. 1982, pp. 1-10.
- Sandhu, K.S. and Jain, S.P. : "Steady State Operation of Self-Excited Induction Generator with Varying Wind Speeds", International Journal of Circuits, System and Signal Processing, Issue, Vol. 2, 2008, pp. 26-33.
- Nassereddine, M., Rizk, J. and Nagrial, M. : "Switching Reluctance Generator for Wind Power Applications", World Academy of science, Engineering and Technology, 41, 2008, pp. 126-130.
- Adel. S. Nada: "Analysis And Control of a Wind Energy Driven Self-Excited Induction Generator Connected to an infinite Bus Bar", PH.D Thesis, Al-Azhar University, Cairo, 2000.
- Say, M.G.: "Alternating Current Machines", Fourth Edition, London, Pitman (ELBS) 1976.
- Fitzgerald, Kingsley and S. D. Umans: "Electrical Machinery", McGraw Hill, New-York, 2003.
- Lander, W.: "Power Electronics", McGraw Hill, London, 1981.
- Muhammad H. Rashid: "Power Electronics Circuits, Devices and Application", Third Edition, Prentice-Hall, Englewood Cliffs, New Jersey, 2004.
- Gary, L. Johnson: "Wind Energy System", Prentice-Hill & Inc., 1985.

5/12/2013