Multiple Access Communication System Using Orthogonal Lu Chaotic Vector

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Abstract: The multiple access techniques based on chaotic signals suffer from high co-channel interference due to pseudo-orthogonal nature of chaotic signals. In this paper, an efficient chaotic multiple access communication system based on Orthogonal Chaotic Vector (OCV) generated from Lu system has been proposed. To measure the effectiveness of the proposed system, its performance has been compared with traditional code division multiple access system (CDMA) based on Walsh-Hadamard sequence which has perfect orthogonally. The simulation results showed that the proposed scheme successfully separates the messages of each user and its performance is almost the same regardless of the number of users in AWGN channel. The results also showed that for four users and at bit-error-rate of $10^{-3}$, the proposed system has achieved gains of 5 dB and 8 dB in signal-to-noise ratio over traditional CDMA system in AWGN and Rayleigh fading channels respectively.


Keywords: Chaotic signals; multiple access; Lu system; orthogonal chaotic vector.

1. Introduction

Many researches have shown the effectiveness of applying chaotic sequences in multiple access digital communication systems to replace the pseudo-orthogonal binary code sequences (Jovic et al., 2007; Lau et al., 2002; Coulon and Roviras, 2009; Tam et al., 2004; Lu, 2005; He and Leung, 2005). For multiple access systems, sequences with low cross-correlation properties are required. Such sequences can be generated using chaotic systems with different initial conditions. The first proposal for possible use of chaotic sequences in multiple access systems is presented in (Heidari-Banteni and McGillem, 1992) followed by some other similar proposals (Abel et al., 1997; Elmirghani and Cryan, 1995; Kohda and Tsuneda, 1994; Yang and Chau, 1997). The performance of the chaotic CDMA system has been analyzed in Mazzini (Mazzini et al., 2001). They showed that chaos-based sequences can outperform m-sequences & Gold codes.

Some researchers like Tse (Tse, 2005) warned that annotating engineering solutions with chaos terminologies may divert reviewers’ attention away from comparing with conventional methods. Also researchers tend to present themselves very positively in talking about chaos. Thus potential advantages of chaotic solutions are emphasized, but difficult problems are often not discussed adequately. In case of CDMA systems, the current conventional spreading codes used in the 3G systems are the orthogonal Walsh codes. For such systems, it has been recognized (although generally not published) that the chaotic codes cannot beat the orthogonal codes in AWGN environment. However, because of the rather bad auto-correlation properties of the orthogonal codes, there should be cases in multipath channel environment, in which chaotic codes outperform orthogonal codes.

Orthogonal Chaotic Vector (OCV) (Venkatesh and Singh, 2011) is an efficient way to generate orthogonal chaotic sequences that has good auto-correlation properties beside the good cross-correlation properties. Unfortunately, publications on the performance comparison of chaotic multiple access based on OCV with traditional CDMA based on orthogonal spreading codes are rare. Probably because it is commonly recognized that orthogonal spreading codes will generally outperform chaos map spreading codes. Furthermore, the little existing works considered the use of chaotic maps for multiple access although the chaotic flows like Lu are easier to be generated practically from physical electronic circuit. In this work, multiple access communication system based on the OCV of Lu flow sequences has been proposed and simulated. A random time-invariant multipath channel is used for BER simulations. The receiver is a RAKE receiver with enough fingers to capture all the energy from the multipath. Perfect channel estimation is assumed, and only downlink multiuser cases are simulated.

The rest of the paper is organized as follows: Section 2 describes the architecture of the proposed system. Section 3 presents the Lu system and OCV generation. The performance of the proposed system over AWGN and fading channels are given in sections 4 and 5 respectively. Finally, the simulation results and conclusions are presented in sections 6 and 7 respectively.
2. The proposed system structure

![Diagram of the proposed chaotic multiple access system based on Lu model. (a) the transmitter, (b) the receiver.]

The block diagram of the proposed multiple access system based on Lu OCV system is shown in Figure 1. In the transmitter, for each one of the \( N_u \) users the data \( d^{(j)} \) for the \( j \)th user are generated using the random data generator and then modulated using BPSK modulator (QPSK or other digital modulation schemes can also be used). The modulated data \( d^{(j)} \) for the \( j \)th user are spread using unique Lu chaotic sequence. The Lu sequences are generated by entering one of the outputs of Lu system to OCV circuitry to generate \( N_u \) orthogonal Lu sequences for \( N_u \) different users. The spreading operation is simply a multiplication process between the chaotic sequence and the BPSK modulated signal. The spread signals are added to each other and sent though the transmission channel. At the receiver, each of the \( N_u \) received signals is despread by multiplying it by the same chaotic signal replica used at the transmitter of the corresponding user. The energy produced by despread signal is detected by an integrate and dump operation followed by a threshold based decision circuit. Finally the recovered signal is demodulated to obtain the transmitted data.

The main difference between the proposed system and the traditional CDMA system used for wireless applications is that the digital Walsh-Hadamard sequence is replaced by Lu OCV analogue sequence to improve the system performance and capacity.

3. Lu orthogonal chaotic vector

The Lu system (Kemih and Benslama, 2006) is a continuous-time dynamical system which belongs to the autonomous type of dynamical systems. The Lu system is three-dimensional system described by the following differential equations:

\[
\begin{align*}
\dot{x} &= a (y - x) \\
\dot{y} &= -xz + cy \\
\dot{z} &= xy - bz
\end{align*}
\]  

where \([x \ y \ z]\) is the output state vector while \(a\), \(b\) and \(c\) are three real valued parameters. As a three-dimensional system with three parameters, the Lu system can lead to very complicated behavior on changing the parameter values. Choosing the standard parameter values \(a = 36\), \(b = 3\), and \(c = 20\), the attractor is obtained, as shown in Figure 2. The non-zero values of cross-correlation between mutual chaotic sequences (\(x\), \(y\), and \(z\)) of Lu system in chaotic multiple access system result in Multiple Access Interference (MAI) between users. The effect of MAI is increased as the number of users is increased. The effect of MAI problem can be eliminated by applying Gram-Schmidt's ortho-normalization process (Haykin, 1994) on flow chaotic sequence vectors to obtain flow OCVs (\(x\), \(y\) and \(z\)) respectively. Gram-Schmidt ortho-normalization process for \(N_u\) orthogonal chaotic signal generators is given by:

\[
\begin{align*}
\mathcal{Q}_n &= \frac{\mathbf{x}(k)}{\sqrt{\sum_{k=1}^{p} [\mathbf{x}(k)(p) - \sum_{n=1}^{q} \mathbf{x}(k)(p) \mathcal{Q}_n(k)(q)] \mathcal{Q}_n(k)(q)}}
\end{align*}
\]
AWGN, is the sum of modulated OCVs of each user and can be represented by:

\[ r(j) = \sum_{i=1}^{N_u} y_i(j) + n(j) \]  

(7)

where \( n(j) \) is the additive white Gaussian noise with zero mean and \( N_s/2 \) variance. At the receiver, it is assumed that a similar replica of spreading sequence is available and it is exactly synchronized with the transmitted one. The \( m \)th decoded symbol for the \( j \)th user, denoted by \( d_m^{(j)} \), is determined according to the rule:

\[ d_m^{(j)} = \begin{cases} +1, & \text{if } O_m^{(j)} = \sum_{i=1}^{N_u} r(i) f(i) > 0 \\ -1, & \text{if } O_m^{(j)} = \sum_{i=1}^{N_u} r(i) f(i) \leq 0 \end{cases} \]  

(8)

Without the loss of generality, we consider the probability of error for the first symbol. Omitting the subscripts of the variables \( d_m^{(j)} \) and \( O_m^{(j)} \) for the sake of brevity, the decision parameter of the \( j \)th user is given by:

\[ O_m^{(j)} = \sum_{i=1}^{N_u} \left[ f(i) \right]^2 + \sum_{i=k+1}^{N_u} \left[ f(i) \right]^2 + \sum_{k=1}^{N_u} n(i) f(i)^2 \]  

(9)

since chaotic vectors used for each user is ortho-normal to each other, the second term in equation (9) causing MAI will be equal to zero. Assuming, that \( O_m^{(j)} \) has a Gaussian distribution, the BER for \( j \)th user can be written as (Venkatesh and Singh, 2011):

\[ BER^{(j)} = \frac{1}{2} \text{erfc} \left( \frac{E \left( O_m^{(j)} | d_m^{(j)} = +1 \right)}{\sqrt{2 \text{var} \left( O_m^{(j)} | d_m^{(j)} = +1 \right)}} \right) \]  

(10)

where the mean value of \( O_m^{(j)} | d_m^{(j)} = +1 \) is given by:

\[ E \left( O_m^{(j)} | d_m^{(j)} = +1 \right) = \beta E \left[ \left( f(i) y_i^{(j)} \right)^2 \right] = E_b \]  

(11)

where \( E_b \) is energy per bit. The variance is given by:

\[ \text{var} \left[ \sum_{i=1}^{N_u} \left[ f(i) y_i^{(j)} \right]^2 \right] = \beta \frac{N_u}{2} E \left[ \left( f(i) y_i^{(j)} \right)^2 \right] \]
parameters of the generated Lu sequence were a factor is chosen to be 64 in both systems. The with the same simulation parameters has also another simulation model for traditional CDMA Figure 1 has implemented in MATLAB. Besides, OCV Lu based multiple access system shown in 6. Simulation results

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or not. Therefore, the simulation results may give us BER performance of the proposed system is (Venkatesh and Singh, 2011):

per bit) will be chi-

ɣ

fading channel, let α

channel

5. Performance analysis over Rayleigh fading channel

Assuming that the channel is a slow Rayleigh fading channel, let α is a Rayleigh distributed random variable denoting fading gain. Then it can be shown that the BER of jth user in symbol duration is:

BER(j)=\frac{e^{-\frac{y}{\gamma}}}{\gamma} f_{\text{Rayleigh}}(y)

(14)

where

\gamma = \frac{E[\alpha]}{N_0}

(15)

Since α is Rayleigh-distributed random variable, y (the received instantaneous signal to noise ratio per bit) will be chi-square distributed and has the form (Venkatesh and Singh, 2011):

f_{\text{Rayleigh}} = \frac{y^{-\frac{3}{2}} e^{-\frac{y}{\gamma}}}{\gamma^3} \gamma > 0

(16)

where,

\gamma = E[y] = E[\alpha].\frac{E[\beta]}{N_0}

(17)

Therefore, the average BER for jth user is:

BER_{\text{Rayleigh}} = \int_{0}^{\infty} BER(y) f_{\text{Rayleigh}}(y) dy

(18)

The last equation shows that in case of Rayleigh fading channel, there is no clear relation weather the BER performance of the proposed system is independent on the number of users and spread factor or not. Therefore, the simulation results may give us more clear view about this issue.

6. Simulation results

A complete simulation model for the proposed OCV Lu based multiple access system shown in Figure 1 has implemented in MATLAB. Besides, another simulation model for traditional CDMA system based on orthogonal Walsh-Hadamard code with the same simulation parameters has also implemented for the purpose of performance comparison. In all simulation results the spreading factor is chosen to be 64 in both systems. The parameters of the generated Lu sequence were a = 36, b = 3, and c = 20 while the initial conditions were [x0 y0 z0] = [0.05 -0.111 0.9]. The number of users has changed from single user to a maximum of 16 users. The multipath fading channel used is a three tap random time-invariant Rayleigh fading channel (Venkatesh and Singh, 2011).

- **Simulation results in AWGN channel:**

  Figure 4 shows the BER performances of the multiple access system based on OCVs generated from individual outputs of Lu system (x, y, and z) for single user transmission in AWGN channel together with traditional CDMA system. It can be noticed from this figure that the performances of OCVs generated using different outputs of Lu system is not the same. The OCV associated with output y has the best performance. Therefore, it will be selected for all the remaining simulation results. Also it is obvious in this figure that OCVs outperforms the traditional CDMA. For example, at BER=10^{-3}, a gain of 5 dB in E_b/N_0 is obtained.

  Figure 5 depicts the BER performances when the number of users is 4. Once again, the OCV based multiple access system outperforms the traditional CDMA. At BER=10^{-3}, a gain of 5 dB in E_b/N_0 is obtained. The improvement can be attributed to good combination of auto and cross-correlation properties of Lu OCVs. In other word, OCV sequences has ideal auto-correlation properties and acceptable cross-correlation ones while Walsh sequences has ideal cross-correlation properties but worse auto-correlation ones.

  Figure 6 shows the performance of the proposed OCV of Lu based multiple access system with different number of users. It is obvious from this figure that the performance is almost the same regardless of the number of users. This result confirms the conclusion mentioned early in section 4 upon the derivation of equation (13).

- **Simulation results in Rayleigh fading channel:**

  Figure 7 shows the BER performances of CDMA based on OCVs generated from individual outputs of Lu system (x, y, and z) for single user transmission in Rayleigh multipath channel together with traditional CDMA system. It can be seen in this figure that all OCVs generated from different Lu system outperforms the traditional CDMA. However, the best performance results are obtained in the case of output y as it was the case in AWGN channel. At BER=10^{-3}, a gain of 5 dB in E_b/N_0 is obtained.

  Figure 8 shows the BER performance comparison when the number of users is 4. Here, it can be easily noticed that the OCV Lu based multiple access system outperforms the traditional CDMA. The improvement in the case Rayleigh fading channel is more than AWGN case. For instance, at BER=10^{-3}, a
gain of 8 dB in SNR is obtained in Rayleigh fading channel while it was 5 dB in AWGN channel.

Figure 4: Performance of Lu OCV sequences and Hadamard sequence for single user transmission in AWGN channel.

Figure 5: Performance of Lu OCV (sequence y) and traditional CDMA for 4 users transmission in AWGN channel.
Figure 6: Performance of Lu OCV for different number of users in AWGN channel.

Figure 7: Performance of Lu OCV sequences and the Hadamard sequence for single user transmission in Rayleigh fading channel.
Figure 8: Performance of Lu OCV (sequence y) and traditional CDMA for 4 users transmission in Rayleigh fading channel.

Figure 9: Performance of Lu OCV for different number of users in Rayleigh fading channel.

Finally, Figure 9 depicts the performance of the proposed OCV of Lu based CDMA with different number of users. It is obvious from this figure that the performance is improved as the number of users is decreased which is the similar case in traditional CDMA systems. However, this was not the case in AWGN channel where the performance was the same regardless the number of users. But in all cases the performance of the proposed scheme is better than the traditional CDMA for the similar number of users as we have seen for an example case $N_u=4$ in the previous figure.

7. Conclusions

The performance of multiple access system can be significantly improved by the use of OCV
generated from Lu chaotic system using Gram-Schmidt ortho-normalization process as a spreading sequence. OCV has ideal auto-correlation properties and acceptable cross-correlation ones. This good combination is the reason behind its good performance in both AWGN and fading channels as compared with the traditional Walsh-Hadamard sequence which has ideal cross-correlation properties but worse auto-correlation ones. OCVs generated from different Lu system outputs have different performances; so, the one of the best performance should be selected to obtain the best improvement. Finally, as the theoretical analysis and simulation results showed, OCVs have almost the same performance regardless of the number of users or the spreading factor in AWGN which is a unique feature as compared with other multiple access techniques.

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