Acid Washing Of "Zeolite A": Performance Assessment And Optimization

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Abstract Zeolite A has been developed, characterized and tested for the removal of chromium (III) from solutions. To facilitate the industrial manufacture of zeolite A, numerous experimental trials and testing procedures have been undertaken to develop prediction methodology for the synthesis of zeolite A with specified characteristics. However, conditioning of the prepared zeolite to the required pH and purity necessitated extensive washing cycles and time. In this paper an approach has been developed, through modeling and optimization techniques, to predict the range of operating parameters governing the washing of zeolite A using oxalic acid and elucidate the mechanism governing the acid washing process in a batch stirred tank reactor. Several washing parameters have been addressed comprising acid gram equivalent, liquid to solid ratios, temperature and stirring speed. It is thus possible through this prediction methodology to define the conditions required for minimum washing costs and high chromium (III) uptake. Determination of the effectiveness factor indicates that the chemical reaction controls the washing rate. The results of this paper indicate that the amount of water required for washing decreased from 310 m³ to 20 m³ per ton zeolite A using oxalic acid, consequently the washing cost decreased by about 18%. The results of optimization indicate that the acid washed zeolite A was able to adsorb 179 mg Cr³+/g as compared to 184 mg Cr³+/g for the conventionally washed zeolite A. [Journal of American Science 2010; 6(5):261-271]. (ISSN: 1545-1003).

Key words: zeolite A, washing, prediction, optimization, chromium

1. Introduction

Zeolite A has been in environmental practice for decades as an effective tool for the removal of heavy metals. [1-5] With the rapid increase in demand, synthetic routes to zeolites synthesis have been widely explored [6-13] with the aim of setting cost effective approach for the preparation of tailored zeolite [14-19]. According to the conventional manufacturing processes, zeolite A is synthesized in an aqueous environment in presence of NaOH. For the structure of zeolite A to be stable and to be handled safely in several applications such as detergents and adsorbents for heavy metals, etc..., the excess alkalinity should be minimized or eliminated. [20-22]

According to the reported experience, this operation is normally performed by washing with demineralized water in a filter press or centrifuge until almost complete removal of NaOH.[23-25] There are many disadvantages of this procedure, for example, the excessive amount of wash water used and the intensive energy requirements in the filtration and/ or centrifugation of the wash water which increase the cost of this separation process. Further, it is difficult to reach a pH value < 9.5 even by using excessive amounts of washing water. The recovery or treatment of large amounts of washing water

represents another disadvantage. Moreover, after drying, aggregate powders having low apparent density, which are difficult to be handled, are obtained [20].

To improve these short comings several approaches have been reported. Prepared zeolite was separated from the mother liquor, without or by partial washing followed by neutralization of the residual NaOH in the cake by a suitable acid. This solution presents practical difficulties due to the extreme instability of the zeolite in a strong acid environment, with possibilities of dealumination and structure degradation. [20,22]

Acid conditioning has been attempted by different workers. N.G. Vasilev, et.al, used HCl acid treatment of zeolites NaX, NaY, mordenite Na(NaM), and natural aluminosilicate clinoptilolite (NaK). The results of this research confirm that during zeolite treatment by hydrochloric acid there is destruction of the aluminum-oxygen tetrahedra to yield aluminum ions and to form silanol groups. [22]

Sulphuric acid washing has been described in a Japanese patent[26]. The inventors concluded that this process requests substantially critical working conditions. Neutralization has been performed using a suitable fluidizer and sulphuric acid at a concentration greater than 70%. This process did not

give rise to significant alterations in the stability of the neutralized zeolite A.

Moreover, the use of tridecyl benzene sulphonic acid has proved to be very expensive, due to the very large amount of the acid requested for the neutralization step.[27]

In this paper a modified cost effective acid washing method has been developed for neutralization of zeolite A with significant reduction of wash water and complexation and precipitation removal mechanisms of chromium associated with highly alkaline zeolite A. [28]

Oxalic acid has been chosen being an organic weak acid to avoid the strong acidity and severity of acid treatment on zeolite structure. The formed soluble sodium oxalate salt is easily separated with the wash solution. In addition, sodium oxalate is considered as a good dispersant for silicates in solution which aids strongly in the homogeneity and the efficiency of acid washing at all zeolite washed sites. This avoids localization and accumulation of highly acidic sites which may cause structure damage.[20,22

This paper also addresses the development of an approach for the prediction of optimum zeolite A washing conditions required to fulfill high chromium uptake and minimum washing cost based on a model developed from the experimental data followed by optimization. Physical interpretation of the washing data is introduced through diffusion with chemical reaction models and calculation of Thiele modulus.[29,30]

2. Material and Methods

2.1 Materials

Synthesis materials comprise aluminum hydroxide (Panareac Quimicasa), sodium meta silicate (Arabic Laboratory Equipment Co. GPR), sodium hydroxide (Modern Lab) and oxalic acid dihydrate (POch S.A). Zeolite A has been synthesized following the predicted synthesis conditions and the starting molar ratios as described in previous work. [31] Briefly, the synthesis gel has been prepared by addition of the silicate solution to the aluminate solution at 65°C, and mixing for 1 h at 500 rpm with seeding by a previously prepared zeolite of about 7.5 wt%, followed by crystallization for 2 h at 95°C and 250 rpm.

2.2 Washing

Even though solids' washing was achieved by traditional cake washing and displacement techniques, this work introduces a new technique for washing, which is applied in a batch stirred tank reactor. A certain weight of zeolite cake has been placed in oxalic acid solution of varying composition

which is expressed as acid gram equivalent AGE (0.8-1.2). One AGE was determined by using 4.6 ml of 1N oxalic acid dihydrate per gram of zeolite A to reach pH 8.5. The liquid to solid ratio (water ratio WR) was varied in the range (20-120). WR is defined as the water volume (ml) used to wash one gram zeolite A. The mixture was mixed using a mechanical stirrer (VELP Scientifica DLS) with stirring speed varying from 50 to 500 rpm and at temperature ranging of (22-60) °C. After the specified washing time (2 h), the solution has been separated by a centrifuge (Flyng Pharma Apparate TDL-5A). The samples were then dried and sieved.

2.3 Chromium adsorption

The adsorbent (0.1 g), with particle size <75 microns, was left in contact with 100 ml of the chromium sulphate solutions of 1000 ppm with an initial pH value of about 3. The experiments were carried out at room temperature for one hour under constant shaking. The filtered solution was then analyzed to determine the final chromium concentration using an atomic absorption flame spectrometer (GBC Avanta). The adsorption capacity is expressed as the amount of ions adsorbed per unit mass of adsorbent

2.4 Characterization

The chemical formula, phases formed, have been characterized by X-ray diffraction analysis (XRD) using a computer controlled X-ray diffractometer (made by Diano Corporation, USA) of a measuring range (2θ) from -20° to +150°. Target X-ray tube operated at 45 kV and 6 mA. The prepared samples have been also analyzed by X-ray fluorescence analysis (XRF) using AXIOS, WD-XRF Sequential Spectrophotometer (Panalytical, determination of the Si/Al molar ratio. The FTIR spectra of washed zeolite samples was recorded using FTIR spectrophotometer (FT/IR-6100 type A) between 400-1600 cm⁻¹). Zeolite surface morphology has been determined using Scanning Electron Microscope (SEM) images Model JEOL: JXA-840A Electron Probe Micro-analyzer coupled with Energy Dispersive Analysis by X-ray (EDEX). All samples were gold coated prior to measurement. The particle size distribution was determined with LASER scattering particle size distribution analyzer (Horiba LA 950). Zeta potential has been used to characterize the zeolite used at various pH conditions. It was measured using a laser zetameter, Malvern instruments, (Zeta sizer 2000).

2.5 Theoretical analysis

2.5.1 Theoretical models & Optimization

The experimental results have been theoretically analyzed assuming diffusion with chemical reaction mechanism. It is assumed that the occurring reaction was a first order neutralization reaction between the sodium hydroxide which has been entrapped and the added oxalic acid. Calculation of the reaction rate constant and diffusion coefficient were necessary to estimate the value of Thiele modulus and effectiveness factor [29]. The rate equation for a first order reaction could be written as follows:

$$r = k[C - Ce] \quad (1)$$

Where r is expressed as (mol/sec. g zeolite), krepresents the first order reaction rate constant (cm3/sec. g zeolite), C and Ce represent the hydrogen ion concentration at different times and at equilibrium respectively (mol/cm³). The reaction rate constant was determined by parameter estimation using the first order reaction rate equation by firstly performing numerical integration of the rate equation for an initial assumption of the rate constant using the method of Runga-Kutta-Fehlberg [32]. The square of the difference between the calculated and the actual acid concentrations in the range of variation of time is then used as the objective function to calculate an improved value of the rate constant using Marquardt algorithm [33]. This procedure is iteratively repeated using tailored software until the value of the rate constant that provides acceptable error between the calculated and measured acid concentration is obtained. The diffusion coefficient, De (m²/sec), can be estimated by the Wilke-Chang equation [34,35]

$$De=7.4E-15 \frac{T(\xi M)^{0.5}}{\eta(\upsilon*10^{6})^{0.6}}$$
 (2)

Where T is the washing temperature (K), ζ represents the association factor of solvent (water), M represents the solvent's molecular weight, υ represents the solute (sodium hydroxide) molar volume (m³/mol) and η represent the solvent dynamic viscosity (Pa sec). Thiele modulus was then calculated using the following equation:

$$\Phi = \frac{rs}{3} \sqrt{\frac{k\rho}{De}}$$
 (3)

Where Φ is the dimensionless Thiele type modulus for spherical pellet, rs represents zeolite pellet diameter (m), ρ represents the zeolite density (g/cm³) and De is the diffusion coefficient of sodium hydroxide from the zeolite pores out to the washing solution (m²/sec). The effectiveness factor $\hat{\eta}$ was then determined according to Smith. [29]

2.5.2 Empirical models formulation

Empirical models were formulated representing the effect of the different washing parameters on the final washing pH and on the chromium uptake. The experimental results have been correlated by applying relevant analysis methods, such as multiple non linear regression software and curve fitting to develop empirical models governing the washing of zeolite A. Typical software used for the purpose include Labfit (V.7.2.37) and Microsoft Excel.

2.5.3 Optimization

BOX Complex Routine [36] has been used to predict and define the optimum washing conditions required to fulfill minimum washing cost and high chromium uptake. This has been achieved through formulation of a cost objective function constrained with the formulated empirical equations relating the final washing pH and the chromium uploading to the washing conditions.

3. Results and Discussion

3.1 Characterization 3.1.1 XRD

Figure 1 represents a typical XRD chart for 3 of the prepared zeolite samples and acid washed at different conditions and a sample washed with water till pH 10.4. The XRD chart for the acid washed samples is typical of that of zeolite prepared via the prediction route and washed with distilled water till pH 10.4. The charts show sharp peaks of high intensity indicating highly crystalline and pure zeolite A with the following composition and characteristics: Product name: Na₂O. Al₂O₃. 2SiO₂. 4.5(H₂O)—Sodium aluminum silicate hydrate (Zeolite LTA), molecular weight: 2191.06System: cubic with unit cell parameter a=24.61.[37,38]

This indicates that the acid washed zeolite samples retains the intact zeolite A structure and the identified chemical structure as that of the samples washed with water until pH 10.4

3.1.2 XRF

XRF was also used to emphasize the performed zeolite structure. It resulted in Si/Al ratio of almost 1 for all the acid washed and the conventionally water washed samples, which agrees with the XRD identified Si/Al molar ratio.

3.1.3. Inrfa red spectrometry

Figure 2 displays the FTIR spectra of the washed zeolite samples between (400-1300 cm⁻¹) [6,37]. The IR spectra shows the structure sensitive bands, as follows: asymmetric stretch 995 cm⁻¹, symmetric stretch 600 cm⁻¹, double rings D4R 550 cm⁻¹ which is characteristic of zeolite A [28,37] and T-O bend 464

cm⁻¹. The presented bands are typical for all washed zeolite A samples, which indicate that the zeolite structure remains intact even after acid washing.

3.1.4 **SEM**

The synthesized zeolite samples have been characterized by (SEM) as shown in figure 3 as typical for the washed samples at 1.2 AGE and 500 rpm (a, b, c) and (d) for water washed zeolite sample at room temperature. The SEM figures show that the highly crystalline small zeolite agglomerates formed have the size from a minimum of 0.2 to a maximum of 2 microns as compared to literature [4, 23]. This indicates that the acid washed zeolite samples retain the same surface morphology. It is clear that sample (1) has a wide particle size distribution, while the other samples have a narrow distribution.

3.1.5 Laser particle size analysis

The following table represents the particle size distribution for all the zeolite washed samples. It is clear that sample (1) has a wide particle size distribution. Also, sample 2 has narrower particle size distribution as indicated in the SEM.

Table (1) Laser particle size analysis of the washed zeolite samples

Sample	Mode size (μm)	Size range (μm)
1	10.1	0.9-101.5
2	4.5	1.2-13.2
3	10.1	1-29.1
4	5.5	1-20

3.1.6 Zeta potential

The zeta potential for the zeolite sample washed at 60°C, 80 WR, 500 rpm and 1.2 AGE, and the zeolite sample conventionally washed is manifested in figure (4). The point of zero charge (PZC) is almost the same (at pH 5.4) for both zeolite samples.

3.2 Effect of washing parameters on pH 3.2.1 Time dependence of solution pH at different acid concentrations

Time dependence of solution pH at different acid concentrations along the 2 hours washing period is represented in figure 5 as typical for all the other parameters.

A sharp fall in pH is observed after the first (5-10) minutes. A typical trend was also observed in the time dependence of solution pH relations at different water ratios, temperature and rpm. indicating rather rapid neutralization of entrained alkalinity with oxalic acid. It is assumed that the accessible alkali under the prevailing conditions has almost been entirely

neutralized since minimal pH change has been observed after 24 h as shown in figure 6.

3.2.2 Effect of water ratio

Effect of water ratio (WR) on the final solution pH after 2 and 24 h is shown in figure 7. Inspection of the data shown in figure 7 reveals the almost insignificant change of the final pH for water ratio more than 20. These findings would help reducing the water ratio used to minimum.

3.2.3 Effect of temperature

Effect of temperature on the final solution pH after 2 and 24 h is shown in figure 8. Increasing the temperature of the acid washing solution reveals 2 distinct zones. The first is related to sharp linear decrease of pH up to 30°C. The second zone (segment) manifests moderate linear decrease of pH up to 60°C, the immediate implication of these results is that most of the unreacted alkali is neutralized in the moderate temperature zone (20-30°C). While the remainder is neutralized between 30-60°C. Thus, in industrial practices using washing solution of temperature 30°C is suffice to bring the final washing pH (after 2 h) from 8.5 to about 7.6. These findings also enable thorough monitoring of the final zeolite pH through simple, but, cost effective tools such as acid concentration, water ratio and temperature.

3.2.4 Effect of stirring speed

Effect of stirring rpm on the final solution pH after 2 and 24 h is shown in figure 9. The final pH is almost constant with the variation in the rpm after 2 and 24 h, which confirms as will be shown later, that the neutralization reaction is not diffusion controlled.

3.3 Performance analysis

Acid washed zeolite samples have been tested for the chromium removal. Figures 10(a-d) show the results of the adsorption tests for zeolites subjected to acid wash under the specified conditions.

Figure 10a manifests a rapid fall of chromium loading from 0.8 to 0.9 AGE followed by almost restoration of a high loading capacity in the range of 0.9 to 1.2 AGE The first segment reflects the effect of pH on the surface of zeolite which decreases the extent of complexation mechanism. Further decrease of pH leads to probable improvement of access to zeolite pores and cavities with subsequent improvement of loading capacity. The value of 1.2 AGE was been chosen to be the appropriate acid gram equivalent one.

Figure 10b manifests an increase of chromium loading from 165 mg/g at 20 WR to 183 mg/g at 60 WR. The chromium loading then decreases to 181

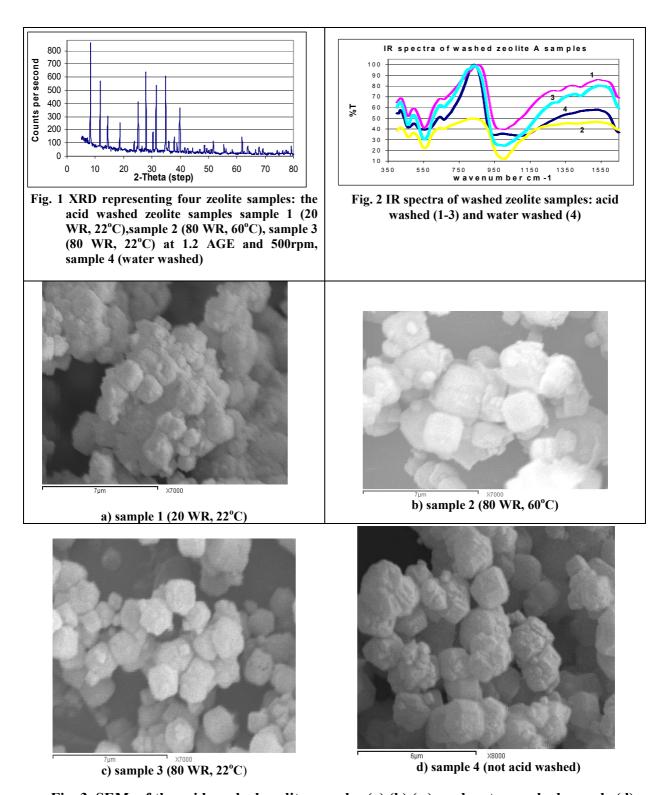


Fig. 3 SEM of the acid washed zeolite samples (a),(b),(c), and water washed sample (d)

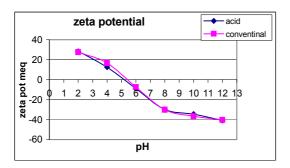


Fig4: Zeta potential measurement of zeolite washed samples

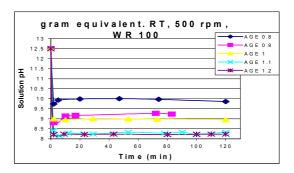


Fig.5: Time dependence of solution pH at different acid gram equivalents at room temperature, 500 rpm and 100 WR

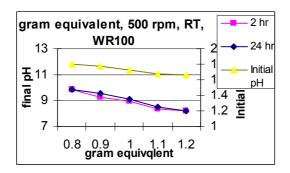


Fig.6: Effect of acid gram equivalent on the final washing pH after 2, 24 hr

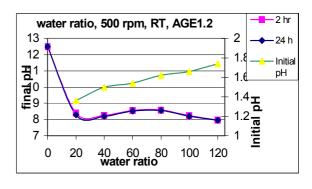


Fig.7: Effect water ratio on the final washing pH after 2, 24 hr

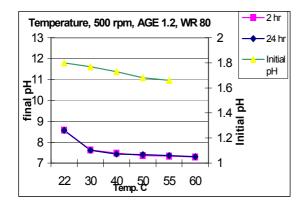


Fig.8: Effect temperature on the final washing pH after 2, 24 hr.

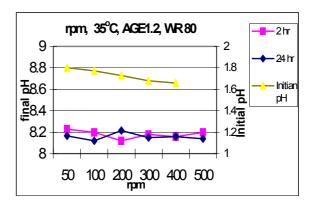


Fig.9: Effect stirring speed on the final washing pH after 2, 24 hr.

mg/g at 80 WR. The value of 80 WR has been chosen to be the most appropriate water ratio. The impact of water ratio is related to simultaneous pH changes and dilution effect. The minor inaccuracies associated with the sensitivity of measurements should be ruled out taking into consideration the narrow range of chromium loading variation (183-170 mg/g).

Figure 10c manifests the decrease of chromium loading from 25°C to 50°C by 7% then it remains almost constant till 60°C. This may be compared with the final pH curve, since the final pH shows moderate to minor decrease above 30°C. Temperature accelerates the alkali neutralization rate which increases the acid washing efficiency. The 7% decrease in the value of chromium loading may be considered minor indicating the limited effect of temperature on the washing process. The value of 35°C has been chosen to be the most appropriate washing temperature.

Table (2) Thiele modulus & effectiveness factor values

<u>Parameter</u>		<u>Value</u>		
I. Input				
T	Temperature (K)	298		
M	Water molecular weight (g/mol)	18		
ζ	Water association factor	2.6		
υ	Solute molar volume (m³/mol)	20 E-06		
rs	Zeolite pellet diameter (m)	2 E-06		
ρ	Zeolite hydrated density (g/cm ³)	2		
II. Calculated				
k	Reaction rate constant (cm³/sec. g zeolite)	5.12 E-04		
De	Diffusion coefficient (m ² /sec)	2.5 E-09		
Φ	Thiele modulus	4.3 E-04		
ή	Effectiveness factor	1		

Figure 10d manifests the sharp increase of chromium loading from 166 mg/g at 50 rpm to 179 mg/g at 200 rpm followed by sharp decrease in the chromium loading for higher rpm. This may be attributed to increasing the ion mobility and homogeneity in mixed solutions up to 200. By increasing the rpm higher than 200 rpm, adsorption and desorption take place simultaneously reducing the over all chromium uptake. The corresponding final washing pH remains almost constant indicating the negligible effect of stirring on the final washing pH.

Figure 11 represents the over all effect of the final pH along the washing study on the chromium loading washing pH. The highest reported value of chromium loading was recorded at final pH value of 9.88. The effect of pH on the Cr(III) adsorption is quite complicated as mentioned by [39]. It was mentioned

that the presence of chromium hydroxide complex is low up to pH 6 then it increases and then decreases again by increasing the pH more than 12. In this study it is worth mentioning that the starting pH of adsorption bulk solution was 3 and it ended at about 4.5-5, which eliminated the complexation precipitation removal mechanism. On the other hand, the actual pH inside the zeolite pores was that of the final washing pH resulting in different forms of chromium complexes other than in bulk solution and enhancing the complexation precipitation removal mechanism inside the pores. The water washed zeolite (sample 4) recorded 184 mg Cr/g zeolite adsorption capacity. It was found that the complexation mechanism has decreased by 14% for some of the acid washed samples.

3.4 Diffusion with chemical reaction

The diffusion with chemical reaction concept was applied to a chosen set of washing conditions as an example for the process. The operating conditions are 1.2 AGE, WR 80, 500 rpm stirring speed and 25°C temperature. The hydrogen ion concentration has been varied from 0.95E-13 to 2.7E-12 mol/cm³ starting from 1 min washing time up to 34 min. The parameters in the previous equations (1-3) were calculated considering a spherical zeolite pellet. The results are shown in the table (2).

The results manifest that the effectiveness factor is considered 1, since Thiele modulus value is less than 1 [29]. This indicates that the rate for the whole zeolite pellet is the same as the rate if all of the surface were available to reactant; i.e., the rate at the center is the same as the rate at the outer surface, consequently the entire surface is considered fully effective and the intraparticle diffusion resistance is minimum. Thus the intraparticle mass transport has no effect and the chemical reaction controls the washing rate. This indicates that the effect of the mixing speed on the washing process is limited for values above 200 rpm. This result was emphasized experimentally as demonstrated in figure (10d).

3.5 Empirical Modeling and optimization

Data analysis has resulted into the formulation of the following empirical equations governing the relationship between the final washing pH, chromium loading and the washing operating conditions and the with R^2 ranging from 0.9 to 1,

$$pH_F = (1.8637 - 0.9643 AGE - 0.0626 WR - 0.25 T - 0.0649 S)^{0.5}$$
 (4)

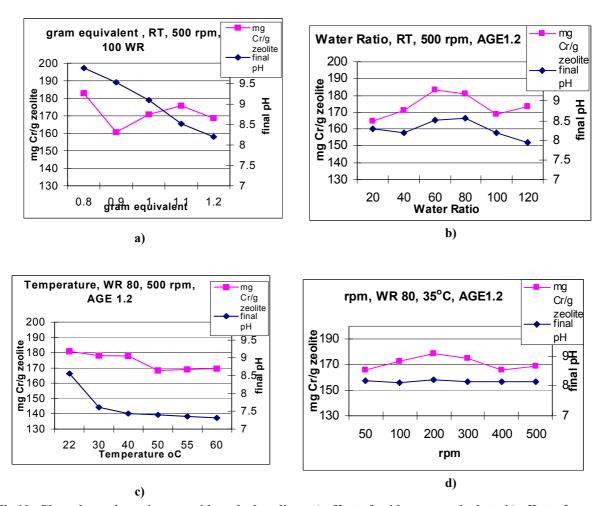


Fig.10: Chromium adsorption on acid washed zeolites: a) effect of acid gram equivalent, b) effect of water ratio, c) temperature dependence and d) influence of rpm

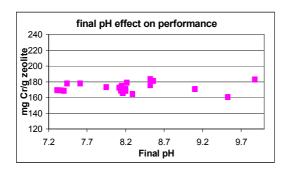


Fig 11: Effect of the final washing pH on the chromium adsorption capacity along the entire washing region

$$L = 30.18 pH_F^5 - 1283.47 pH_F^4 + 21771.52 pH_F^3 - 184166.19 pH_F^2 + 776905.33 pH_F -1307394.33$$
 (5)

BOX COMPLEX routine has been adopted to find the values of the washing conditions that would minimize the washing process costs while maintaining high zeolite chromium loading. This has been achieved through formulation of a cost objective function, equation (6), constrained by equation (4) starting with the pH_F value corresponding to maximum loading calculated from equation (5). Consequently, equations (4) have been used to calculate other parameters using the defined optimum for the independent variables. The objective function is expressed based on the oxalic acid price of 0.2 USD/kg, water price of 0.2 USD/m³, and 0.08 USD/kWh:

$$C = 0.059 \ AGE + 2E-04 \ WR + (4.3E-04 \ AGE+9E-05 \ WR) \ (T-22)$$
 (6)

Results are presented in table (3)

Table (3) Predicted Washing Variables

PARAMETER		RANGE OF VALIDITY	PREDICTED VALUE
pH_F	Final washing pH	(7.31-9.88)	9.87
AGE	Oxalic acid gram equivalent/ g zeolite	(0.8-1.2)	0.8
WR	Water ratio ml/ g zeolite	(20-120)	20
T	Washing temperature (°C)	(22-60)	22
S	Stirring rpm	(50-500)	50
L	Chromium loading mg Cr ³⁺ /g zeolite	(160.6-183)	178.9
С	Washing cost USD/ kg zeolite		0.051
СТ	Washing cost USD/ ton zeolite		51

Table (3) indicates that the oxalic acid demand is about 200 kg/ ton zeolite and the wash water demand

was 20 m³/ ton zeolite. The results show that 51 USD are needed for acid washing of one ton zeolite to a final pH of 9.88. On the other hand 62 USD, represent the price of water only (310 m³/ ton zeolite), for washing of one ton zeolite with water to a pH of 10.4. The net savings are considered to be about 11 USD per ton of zeolite, in addition to other technical benefits as discussed in the previous sections.

4. Conclusions

Zeolite A washed by oxalic acid has been characterized by XRD, XRF, FTIR, SEM, laser particle size analysis and zeta potential measurements. Further, the adsorption capacity of chromium has been assessed The results indicate that the proposed acid washing scheme retained the intact zeolite structure and surface morphology and also high chromium loading as compared to zeolite washed with distilled water. The complexation effect decreased by 14%. The intraparticle mass transport has no effect and the chemical reaction controls the washing rate. This indicates that the effect of the mixing speed on the washing process could be considered negligible above 200 rpm. Based on the adopted optimization procedure, the amount of water required for washing has been decreased from about 310 m³/ ton zeolite to reach pH value of 10.4 to about 20 m³/ ton zeolite with the proposed acid washing scheme to reach pH value range of 9.87. This results in the decrease of the cost & energy requirements of washing process. Consequently the net savings in washing cost has also decreased by about 18% as compared to the conventional zeolite washing conditions. In addition, the formulated rational scheme has proved to be a powerful tool for the prediction of optimum zeolite A washing conditions to fulfil minimum washing cost and high chromium loading.

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